

CIEG 305 HYDROSTATIC FORCES ON CURVED SURFACES

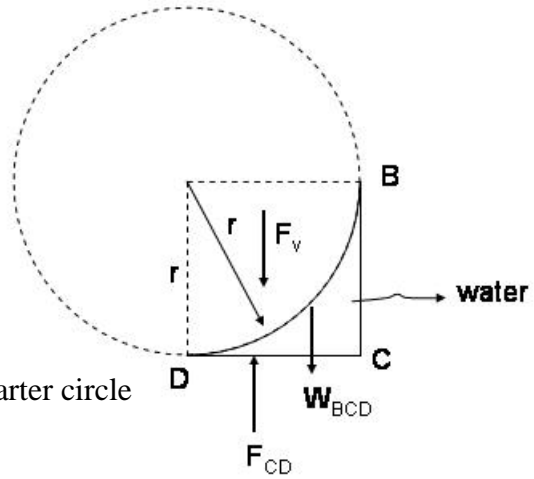
Proof: why does vertical force on curved surface equal weight of fluid above even when the fluid is below?

$$F_{CD} = F_V + W_{BCD}$$

$$F_V = F_{CD} - W_{BCD}$$

$W_{BCD} = \gamma A b$, b equals distance in to paper

$$W_{BCD} = \gamma b \left(r^2 - \frac{\pi r^2}{4} \right), \text{ the square minus the quarter circle}$$



$$F_{CD} = \gamma A = \gamma (rb) = \gamma b r^2$$

THUS

$$F_V = \gamma b r^2 - \gamma b \left(r^2 - \frac{\pi r^2}{4} \right)$$

$$F_V = \gamma b r^2 - \gamma b r^2 + \gamma b \frac{\pi r^2}{4}$$

$$F_V = \gamma b \frac{\pi r^2}{4}, \text{ this is the weight of the fluid above the surface even though it is not there!}$$